## Some solutions to Happy Octopus

$1,1,1, \ldots$ so 1 is happy.
$2,4,20,4,20, \ldots$ so 2 is sad. (2-cycle)
$3,11,2,4,20, \ldots$ so 3 is sad. (2-cycle)
4 is sad. (2-cycle)
$5,31,12,5, \ldots$ so 5 is sad. (3-cycle)
$6,44,40,20,4,20, \ldots$ so 6 is sad. (2-cycle)
$7,61,45,51,32,15,32, \ldots$ so 7 is sad. (2-cycle)
$10,1,1,1,1 \ldots$ so 10 is happy.
$11,2,4,20,4, \ldots$ so 11 is sad. (2-cycle)
$12,5,31,12, \ldots$ so 12 is sad. (3-cycle)
$13,12, \ldots$ so 13 is sad. (3-cycle)
$14,21,5, \ldots$ so 14 is sad. (3-cycle)
$5,32,15, \ldots$ so 15 is sad. (2-cycle)
$16,45,51,32, \ldots$ so 16 is sad. (2-cycle)
$17,62,50,31, \ldots$ so 17 is sad. (3-cycle)
20, 4, 20, 4, ... so 20 is sad. (2-cycle)
$21,5, \ldots$ so 21 is sad. (3-cycle)
$22,10,1,1, \ldots$ so 22 is happy.
$23,15, \ldots$ so 23 is sad. (2-cycle)
24, 24, 24, 24, so 24 is happy.
25, 35, , 42, 24, 24,... so 25 is happy.
$26,50,31, \ldots$ so 26 is sad. (3-cycle)
$27,65,75,112,6,44,40,20, \ldots$ so 27 is sad. (2-cycle)
$30,11,2,4,20, \ldots$ so 30 is sad. (2-cycle)
$31,12, \ldots$ so 31 is sad. (3-cycle)
$32,15, \ldots$ so 32 is sad. (2-cycle)
33, 22, 10, 1, ... so 33 is happy.
$34,31,12, \ldots$ so 34 is sad. (3-cycle)
35, 42, 24, 24, ... so 35 is happy.
$36,55,62,50,31, \ldots$ so 36 is sad. (3-cycle)
$37,72,65,75,112$ so 37 is sad. (2-cycle)
$40>20>4>20$ so 40 is sad. . (2-cycle)
$41,21,5,31,12,5, \ldots$ so 41 is sad. (3-cycle)
$42,24,24, \ldots$ so 42 is happy.
$43,31, \ldots$ so 43 is sad. (3-cycle)
$44,40,20,4,20, \ldots$ so 44 is sad. (2-cycle)
$45,51,32, \ldots$ so 45 is sad. (2-cycle)
46, 64, 64, 64, ... so 46 is happy.
$47,101,2,4,20, \ldots$ so 47 is sad. (2-cycle)

